

EXERCISE 14A**1** Evaluate:

a $\lim_{x \rightarrow 3} (x + 4)$

b $\lim_{x \rightarrow -1} (5 - 2x)$

c $\lim_{x \rightarrow 4} (3x - 1)$

d $\lim_{x \rightarrow 2} (5x^2 - 3x + 2)$

e $\lim_{h \rightarrow 0} h^2(1 - h)$

f $\lim_{x \rightarrow 0} (x^2 + 5)$

2 Evaluate:

a $\lim_{x \rightarrow 0} 5$

b $\lim_{h \rightarrow 2} 7$

c $\lim_{x \rightarrow 0} c$, c a constant

3 Evaluate:

a $\lim_{x \rightarrow 1} \frac{x^2 - 3x}{x}$

b $\lim_{h \rightarrow 2} \frac{h^2 + 5h}{h}$

c $\lim_{x \rightarrow 0} \frac{x - 1}{x + 1}$

d $\lim_{x \rightarrow 0} \frac{x}{x}$

4 Evaluate the following limits:

a $\lim_{x \rightarrow 0} \frac{x^2 - 3x}{x}$

b $\lim_{x \rightarrow 0} \frac{x^2 + 5x}{x}$

c $\lim_{x \rightarrow 0} \frac{2x^2 - x}{x}$

d $\lim_{h \rightarrow 0} \frac{2h^2 + 6h}{h}$

e $\lim_{h \rightarrow 0} \frac{3h^2 - 4h}{h}$

f $\lim_{h \rightarrow 0} \frac{h^3 - 8h}{h}$

g $\lim_{x \rightarrow 1} \frac{x^2 - x}{x - 1}$

h $\lim_{x \rightarrow 2} \frac{x^2 - 2x}{x - 2}$

i $\lim_{x \rightarrow 3} \frac{x^2 - x - 6}{x - 3}$

EXERCISE 14B

1 For each of the following functions:

i discuss the behaviour near the asymptotes and hence deduce their equations

ii state the values of $\lim_{x \rightarrow -\infty} f(x)$ and $\lim_{x \rightarrow \infty} f(x)$.

a $f(x) = \frac{1}{x}$

b $f(x) = \frac{3x - 2}{x + 3}$

c $f(x) = \frac{1 - 2x}{3x + 2}$

d $f(x) = \frac{x}{1 - x}$

e $f(x) = \frac{x^2 - 1}{x^2 + 1}$

f $f(x) = \frac{x}{x^2 + 1}$

2 a Sketch the graph of $y = e^x - 6$.

b Hence discuss the value and geometric interpretation of:

i $\lim_{x \rightarrow -\infty} (e^x - 6)$

ii $\lim_{x \rightarrow \infty} (e^x - 6)$

3 Find, if possible, $\lim_{x \rightarrow -\infty} (2e^{-x} - 3)$ and $\lim_{x \rightarrow \infty} (2e^{-x} - 3)$.